

Math 115

Fall 2018

Lecture 23

$$\begin{array}{c} ? a^2 + b^2 = c^2 ? \\ y = mx + b \quad ? d = rt \end{array}$$

Feb 19-8:47 AM

Factor Completely:

$$\begin{aligned} \textcircled{1} \quad x^5 - 25x^3 &= x^3(x^2 - 25) \\ &= x^3(x^2 - 5^2) = \boxed{x^3(x+5)(x-5)} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad x^3 + 2x^2 - 4x - 8 &= x^2(x+2) - 4(x+2) \\ &= (x+2)(x^2 - 4) \\ &= (x+2)(x+2)(x-2) = \boxed{(x+2)^2(x-2)} \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad x^2(x+3) - 5x(x+3) + 6(x+3) \\ &= (x+3)(x^2 - 5x + 6) \\ &= \boxed{(x+3)(x-2)(x-3)} \end{aligned}$$

Dec 3-6:03 AM

④ $x^2 - 2x - 15 = \underbrace{x^2 - 5x}_{-15} + \underbrace{3x - 15}_{-15}$
 $P = -15$
 $S = -2$
 $-5, 3$
 $= x(x-5) + 3(x-5) = \boxed{(x-5)(x+3)}$

⑤ $x^2 - 2xy - 3y^2 = \underbrace{x^2 - 3xy}_{-3} + \underbrace{1xy - 3y^2}_{-3}$
 $P = -3$
 $S = -2$
 $-3, 1$
 $= x(x-3y) + y(x-3y)$
 $= \boxed{(x-3y)(x+y)}$

⑥ $4x^5 - 28x^4 + 40x^3$
 $= 4x^3(x^2 - 7x + 10)$

$= \boxed{4x^3(x-2)(x-5)}$

Dec 3-6:12 AM

⑦ $2x^2 - 5x - 12 = \underbrace{2x^2 - 8x}_{-24} + \underbrace{3x - 12}_{-24}$
 $P = -24$
 $S = -5$
 $-8, 3$
 $= 2x(x-4) + 3(x-4)$
 $= \boxed{(x-4)(2x+3)}$

⑧ $2x^2 + 7x + 6 = \underbrace{2x^2 + 4x}_{12} + \underbrace{3x + 6}_{12}$
 $P = 12$
 $S = 7$
 $4, 3$
 $= 2x(x+2) + 3(x+2)$
 $= \boxed{(x+2)(2x+3)}$

⑨ $6x^2 - 11x + 3 = \underbrace{6x^2 - 2x}_{18} + \underbrace{-9x + 3}_{18}$
 $P = 18$
 $S = -11$
 $-2, -9$
 $= 2x(3x-1) - 3(3x-1)$
 $= \boxed{(3x-1)(2x-3)}$

Dec 3-6:24 AM

$$(10) \quad x^3 - 49x$$

$$= x(x^2 - 49) = \boxed{x(x+7)(x-7)}$$

$$(11) \quad 81x^2 - 36 = 9(9x^2 - 4)$$

$$= 9[(3x)^2 - (2)^2] = \boxed{9(3x+2)(3x-2)}$$

$$(12) \quad x^4 + 125x$$

$$= x(x^3 + 125)$$

$$= x(x^3 + 5^3)$$

$$= \boxed{x(x+5)(x^2 - 5x + 25)}$$

$$(13) \quad 2x^5 - 16x^2$$

$$= 2x^2(x^3 - 8)$$

$$= 2x^2(x^3 - 2^3)$$

$$= 2x^2(x-2)(x^2 + 2x + 4)$$

Dec 3-6:37 AM

$$(14) \quad 36x^2 - 60x + 25 = (6x - 5)^2$$

$\swarrow \quad \searrow$
 $2 \cdot 6x \cdot 5$

$$(15) \quad 18x^2y + 48xy^2 + 32y^3$$

$$= 2y(9x^2 + 24xy + 16y^2) = 2y(3x + 4y)^2$$

$\swarrow \quad \searrow$
 $2 \cdot 3x \cdot 4y$

$$(16) \quad 81x^2 - 198x + 121$$

$$= (9x - 11)^2$$

$\swarrow \quad \searrow$
 $2 \cdot 9x \cdot 11$

Dec 3-6:49 AM

Solving Polynomial Equations

- 1) Make RHS Zero.
- 2) Factor the LHS Completely.
- 3) use Zero-Factor Property, and Solve all factors.
- 4) Final Ans in Solution Set.

Zero-Factor Prop.:

If $A \cdot B = 0$, then $A = 0$ or $B = 0$ or both are zero.

Dec 3-7:42 AM

Solve $(x-1)(x+8)=0$

RHS=0✓ LHS Completely factored✓

By Z.F.P. $\Rightarrow x-1=0$ or $x+8=0$

$$\boxed{x=1}$$

$$\boxed{x=-8}$$

$$\{-8, 1\}$$

Solve $(2x-5)(3x+4)=0$

RHS=0✓

LHS Factored Completely✓

By Z.F.P.

$$2x-5=0$$

$$2x=5$$

$$\boxed{x=\frac{5}{2}}$$

$$\text{or } 3x+4=0$$

$$3x=-4$$

$$\boxed{x=-\frac{4}{3}}$$

$$\left\{-\frac{4}{3}, \frac{5}{2}\right\}$$

Dec 3-7:45 AM

Solve $x^2 + 6 = 5x$

Make RHS=0 $x^2 + 6 - 5x = 0$

Factor LHS $x^2 - 5x + 6 = 0$

$$(x - 2)(x - 3) = 0$$

By Z.F.P.

$$x - 2 = 0 \quad \text{or} \quad x - 3 = 0$$

$$\boxed{x = 2}$$

$$\boxed{x = 3}$$

Soln Set

$$\{2, 3\}$$

Dec 3-7:50 AM

Solve $2x^2 + 20 = 13x$

1) RHS=0 $2x^2 + 20 - 13x = 0$

2) order,
simplify,
factor

$$2x^2 - 13x + 20 = 0$$

$$P = 40$$

$$S = -13$$

$$-8, -5$$

$$40$$

$$2x^2 - 8x - 5x + 20 = 0$$

$$2x(x - 4) - 5(x - 4) = 0$$

3) use Z.F.P.

$$(x - 4)(2x - 5) = 0$$

$$x - 4 = 0$$

$$2x - 5 = 0$$

4) Solution Set $\left\{\frac{5}{2}, 4\right\}$

$$\boxed{x = 4}$$

$$\boxed{x = \frac{5}{2}}$$

Dec 3-7:52 AM

Solve $x^2 = x + 30$

$$x^2 - x - 30 = 0$$

$$(x - 6)(x + 5) = 0$$

By Z.F.P.,

$$x - 6 = 0 \quad \text{or} \quad x + 5 = 0$$

$$\boxed{x = 6}$$

$$\boxed{x = -5}$$

$$\{-5, 6\}$$

Dec 3-7:57 AM

Solve $2x^2 = x + 6$

$$2x^2 - x - 6 = 0$$

$$P = -12$$

$$S = -1$$

$$-4 \text{ \& } 3$$

$$\left\{-\frac{3}{2}, 2\right\}$$

$$2x^2 - 4x + 3x - 6 = 0$$

$$2x(x - 2) + 3(x - 2) = 0$$

$$(x - 2)(2x + 3) = 0$$

By Z.F.P.

$$x - 2 = 0 \quad \text{or} \quad 2x + 3 = 0$$

$$\boxed{x = 2}$$

$$\boxed{x = -\frac{3}{2}}$$

Dec 3-8:00 AM

Solve $x^2 = 24 - 5x$

$$x^2 - 24 + 5x = 0$$

$$x^2 + 5x - 24 = 0$$

$$(x + 8)(x - 3) = 0$$

By Z.F.P.

$$x + 8 = 0 \quad \text{or} \quad x - 3 = 0$$

$$\boxed{x = -8}$$

$$\boxed{x = 3}$$

$$\{-8, 3\}$$

Dec 3-8:05 AM

Solve $x(x + 7) = 30$

$$x^2 + 7x = 30$$

$$x^2 + 7x - 30 = 0$$

$$(x + 10)(x - 3) = 0$$

By Z.F.P.

$$x + 10 = 0 \quad x - 3 = 0$$

$$x = -10$$

$$x = 3$$

$$\{-10, 3\}$$

Dec 3-8:09 AM

Solve $(2x+3)(x+4) = 25$

Foil & Simplify

$$2x^2 + 8x + 3x + 12 = 25$$

$$2x^2 + 11x + 12 = 25$$

RHS = 0, Simplify

$$2x^2 + 11x + 12 - 25 = 0$$

$$2x^2 + 11x - 13 = 0$$

Factor LHS

Completely

By Z.F.P.

$$2x+13=0 \quad \text{or} \quad x-1=0$$

$$\boxed{x = -\frac{13}{2}}$$

$$\boxed{x=1}$$

$$\left\{-\frac{13}{2}, 1\right\}$$

$$P = -26$$

$$S = 11$$

$$-2, 13$$

$$-26$$

$$2x^2 + 13x - 2x - 13 = 0$$

$$x(2x+13) - 1(2x+13) = 0$$

$$(2x+13)(x-1) = 0$$

Dec 3-8:12 AM

Solve $3x(x+1) = (2x+3)(x+1)$

Hint: Distribute & Foil, then Simplify

$$3x^2 + 3x = 2x^2 + 2x + 3x + 3$$

$$\underline{\underline{3x^2}} + \cancel{3x} - \underline{\underline{2x^2}} - 2x - \cancel{3x} - 3 = 0$$

$$x^2 - 2x - 3 = 0$$

$$(x-3)(x+1) = 0$$

By Z.F.P.

$$x-3=0$$

$$\boxed{x=3}$$

$$x+1=0$$

$$\boxed{x=-1}$$

$$\{-1, 3\}$$

Dec 3-8:19 AM

Solve $x^2 = 100$

$$x^2 - 100 = 0$$

$$x^2 - 10^2 = 0$$

$$(x + 10)(x - 10) = 0$$

by Z.F.P.

$$x + 10 = 0$$

$$x - 10 = 0$$

$$\boxed{x = -10}$$

$$\boxed{x = 10}$$

$$\{-10, 10\} \text{ or } \{\pm 10\}$$

Dec 3-8:26 AM

Solve $36x^2 - 49 = 9$

$$36x^2 - 49 - 9 = 0$$

$$36x^2 - 49 = 0$$

$$(6x)^2 - (7)^2 = 0$$

$$(6x + 7)(6x - 7) = 0$$

By Z.F.P.

$$6x + 7 = 0$$

$$6x - 7 = 0$$

$$6x = -7$$

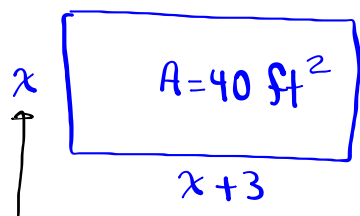
$$6x = 7$$

$$\boxed{x = -\frac{7}{6}}$$

$$\boxed{x = \frac{7}{6}}$$

$$\left\{\pm \frac{7}{6}\right\}$$

Dec 3-8:28 AM

Find x :Can x be negative?

NO

$$\boxed{x=5}$$

$$5 \text{ ft} \quad \boxed{A=40 \text{ ft}^2} \quad 8 \text{ ft}$$

Rectangle

$$A = 40$$

$$LW = 40$$

$$x(x+3) = 40$$

$$x^2 + 3x = 40$$

$$x^2 + 3x - 40 = 0$$

$$(x+8)(x-5) = 0$$

By Z.F.P.,

$$x+8=0$$

$$x-5=0$$

$$x=-8$$

$$x=5$$

Dec 3-8:45 AM

The Product of two consecutive integers is 90

Find all such integers.

$$x \text{ \& } x+1$$

$$x(x+1) = 90$$

$$x^2 + x = 90$$

$$x^2 + x - 90 = 0$$

$$(x+10)(x-9) = 0$$

By Z.F.P.

$$x+10=0$$

$$x-9=0$$

$$x=-10$$

$$x=9$$

x	$x+1$
9	10
-10	-9

$$9 \text{ \& } 10$$

or

$$-10 \text{ \& } -9$$

Dec 3-8:49 AM

The product of two consecutive even integers is 80.

Find all such integers.

Solve $x(x+2) = 80$

$$x^2 + 2x = 80$$

$$x^2 + 2x - 80 = 0$$

$$(x+10)(x-8) = 0$$

By Z.F.P.

$$x+10=0$$

$$x = -10$$

$$x-8=0$$

$$x = 8$$

$$x \neq x+2$$

$$x(x+2) = 80$$

x	$x+2$
8	10
-10	-8

$$8 \neq 10$$

or

$$-10 \neq -8$$

Dec 3-8:53 AM

The area of a rectangular shape is 63 m^2 .

Its dimensions are two consecutive odd integers.

Find its dimensions.

$$A = 63$$

$$LW = 63$$

$$x(x+2) = 63$$

$$x^2 + 2x - 63 = 0$$

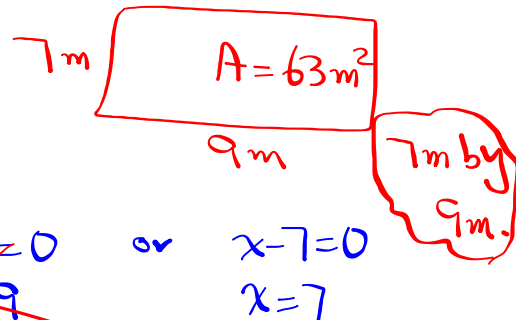
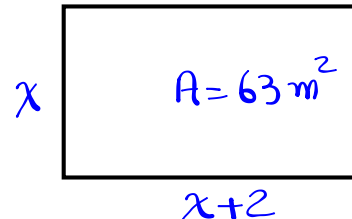
$$(x+9)(x-7) = 0$$

By Z.F.P., $x+9=0$

~~$$x = -9$$~~

or $x-7=0$

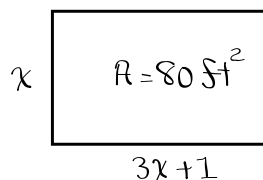
$$x = 7$$



Dec 3-8:59 AM

The area of a rectangular shape is 80 ft^2 .
Its length is 1 ft longer than 3 times
its width.

① Draw & label



② Find its dimensions.

$$A = 80$$

$$LW = 80$$

$$x(3x+1) = 80$$

$$3x^2 + x = 80$$

$$3x^2 + x - 80 = 0$$

$$P = -240$$

$$S = 1$$

$$-15 \div 16$$

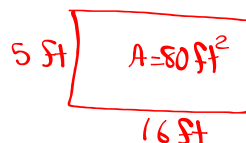
$$-240$$

$$3x^2 - 15x + 16x - 80 = 0$$

$$3x(x-5) + 16(x-5) = 0$$

$$(x-5)(3x+16) = 0$$

$$\text{By Z.F.P.} \Rightarrow \boxed{x=5}, \cancel{x=-16/3}$$



Dec 3-9:04 AM

Factor completely: Box Your Final Answer

① $7x + 14$

$$= \boxed{7(x+2)}$$

② $2xy - 8y + 3x - 12$

$$= 2y(x-4) + 3(x-4)$$

$$= \boxed{(x-4)(2y+3)}$$

③ $x^2 + 6x - 27$

$$= \boxed{(x+9)(x-3)}$$

④ $25x^2 - 121$

$$= (5x)^2 - (11)^2$$

$$= \boxed{(5x+11)(5x-11)}$$

Dec 3-9:11 AM